

Biaxial smectic- A^* phase and its possible misidentification as a smectic- C_α^* phase

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The biaxial smectic- A^* ($\text{Sm-}A_B^*$) phase, appearing in the phase sequence $\text{Sm-}A^*-\text{Sm-}A_B^*-\text{Sm-}C^*$, is analyzed using Landau theory. It is found to possess a helical superstructure with a pitch that is significantly shorter than the pitch of the $\text{Sm-}C^*$ helical superstructure. The $\text{Sm-}A_B^*-\text{Sm-}C^*$ transition can be either first or second order, and correspondingly there will be either a jump or continuous variation in the pitch. The behaviors of the birefringence and electroclinic effect are analyzed and found to be similar to those of a $\text{Sm-}C_\alpha^*$ phase. As such, it is possible that the $\text{Sm-}A_B^*$ phase could be misidentified as a $\text{Sm-}C_\alpha^*$ phase. Ways to distinguish the two phases are discussed.

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Liquid crystals are a fascinating class of materials exhibiting a range of phases (intermediate between liquid and crystalline) which can be classified according to their broken symmetries. The rich variety of their order parameters and phase transitions has led to considerable interest in their properties [1]. In condensed-matter physics they provide an opportunity to study fundamental issues such as the interplay of different types of order, and the effects of chirality on phases and phase transitions, particularly among chiral smectic (Sm^*) phases. There is a rich variety of such phases, which are typically made up of elongated molecules and have a density periodic in one dimension (\hat{z}), that is, layering [2]. As shown in Fig. 1, $\text{Sm-}A^*$ phases have an average molecular long axis (\hat{n}) parallel to the layer normal (\hat{z}). In lower temperature $\text{Sm-}C^*$ phases \hat{n} is tilted by an angle θ from \hat{z} . This tilt can be induced by an electric field, a chiral phenomenon known as the electroclinic effect (EE) [3–5]. The EE allows for rapid switching of the optical axis (\hat{n}), an important feature for electro-optical devices. The chirality of the $\text{Sm-}C^*$ phases results in a helical precession (along \hat{z}) of \hat{n} , with pitch p_C larger than the layer spacing. Thus, as well as layering, $\text{Sm-}C^*$ phases have a helical superstructure which can be probed by Bragg scattering.

The discovery [3] of the EE has led to the ongoing synthesis of an enormous number of chiral liquid crystal compounds with smectic phases, also known as ferroelectric liquid crystals. A large fraction of these compounds display a variety of short pitch $\text{Sm-}C^*$ phases (as well as the conventional, longer pitch $\text{Sm-}C^*$ phase). The “ferrielectric” (ferri) phases (e.g., $\text{Sm-}C_{FI1}^*$ and $\text{Sm-}C_{FI2}^*$, with pitches of three and four layers, respectively) are believed to result from a competition between ferro- and antiferroelectric interactions [6]. As such, they are analogous to ferrimagnetic phases and have been modeled with competing nearest- and next-nearest-layer interactions [6], an example of how a single, fundamental aspect of physics can result in a similar effect in two ostensibly very different systems (magnetic and liquid crystalline). There has also been significant interest [6] in the $\text{Sm-}C_\alpha^*$ ferroelectric phase, which has a pitch between that of the ferri and conventional $\text{Sm-}C^*$ phases. However, unlike the ferri phases, its pitch is incommensurate with the layer spacing. It and the ferri phases appear in the phase sequence $\text{Sm-}A^*-\text{Sm-}C_\alpha^*-\text{Sm-}C^*-\text{Sm-}C_{FI2}^*-\text{Sm-}C_{FI1}^*$, with the $\text{Sm-}A^*$

phase at highest temperature. The short pitch nature of the $\text{Sm-}C_\alpha^*$ phase would naturally lead one to first suspect (as many have [6]) that, like the ferri phases, it is simply another phase with competing interactions.

In this paper we present the first analysis of the chiral biaxial smectic- A^* ($\text{Sm-}A_B^*$) phase [7,8]. The $\text{Sm-}A_B^*$ and $\text{Sm-}C_\alpha^*$ phases have common features: a short pitch helical superstructure, a strong EE effect above the transition to the $\text{Sm-}C^*$ phase and also a strong decrease in birefringence below the transition from the $\text{Sm-}A^*$ phase. Thus, we suggest that in *some* cases a short pitch phase, appearing between the $\text{Sm-}A^*$ and $\text{Sm-}C^*$ phases, could be mistaken for a $\text{Sm-}C_\alpha^*$ phase when it is really a $\text{Sm-}A_B^*$ phase. We show that the unusually short pitch and the strong EE of the $\text{Sm-}A_B^*$ phase are not due to competing interactions but are due instead to completely different basic physics, namely, the distinct symmetries (D_{2h} and C_{2h}) of the $\text{Sm-}A_B^*$ and $\text{Sm-}C^*$ phases. Aside from its obvious scientific and technological importance in terms of better understanding ferroelectric liquid crystals, this result has a broader significance in terms of the subtleties of phase transitions and phase identification. It demonstrates that two very similar phases can occur for two fundamentally different reasons, competing interactions ($\text{Sm-}C_\alpha^*$) and symmetry breaking ($\text{Sm-}A_B^*$). In such cases one must be careful to devise methods of distinguishing between two ostensibly similar phases, and we indeed provide such methods.

That, in *some* cases, the supposedly observed $\text{Sm-}C_\alpha^*$ phase may really be the $\text{Sm-}A_B^*$ phase is also important given that two features of the $\text{Sm-}C_\alpha^*$ are puzzling from the point of view of general condensed-matter physics. In some materials [10,11] the $\text{Sm-}C_\alpha^*-\text{Sm-}C^*$ phase transition has been observed to be continuous. This would contradict the basic tenet that transitions between phases of the same symmetry must be first order [12]. Another puzzling feature of the $\text{Sm-}C_\alpha^*$ phase is its location in the above phase sequence. One would reasonably expect that the phase sequence of symmetrically equivalent phases should occur in order of decreasing pitch and, therefore, that the $\text{Sm-}C_\alpha^*$ phase should appear between the $\text{Sm-}C^*$ and the $\text{Sm-}C_{FI2}^*$ phases. The existence of a $\text{Sm-}A_B^*$ phase could resolve these issues. It and the $\text{Sm-}C^*$ phases are symmetrically distinct and a continuous phase transition between the two is permitted. Also, its location in the phase

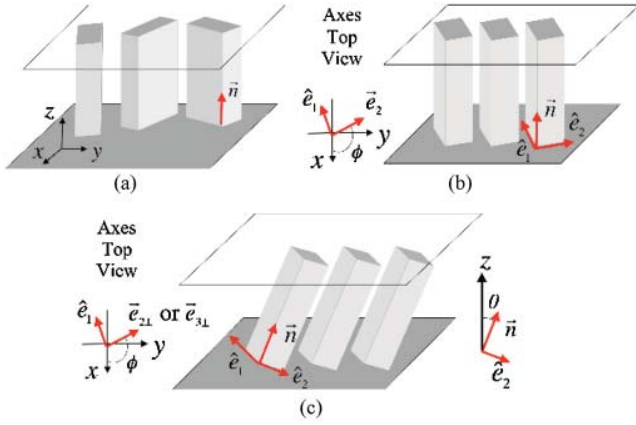


FIG. 1. (Color online) Schematics of (a) Sm-A*, (b) Sm-A_B^{*}, and (c) Sm-C* phases. In each case a single layer is shown. \hat{e}_1 , \hat{e}_2 , and \hat{n} are the eigenvectors of the orientational order tensor.

sequence is consistent with it having symmetry between that of the Sm-A* and Sm-C* phases.

We first discuss the key features of the Sm-A_B^{*} phase, along with ways to distinguish it from the Sm-C* phase. As shown in Fig. 1, the Sm-A_B^{*} phase is nontilted (i.e., $\hat{n} \parallel \hat{z}$) with a special axis picked out *within* the layers. This *axis* is usually specified by a biaxial director \hat{e}_1 but we note that the Sm-A_B^{*} phase possesses intralayer inversion symmetry (i.e., \hat{e}_1 and $-\hat{e}_1$ equivalence). In Sm-C* phases the tilted \hat{n} picks out a special *direction* $\mathbf{c} = \hat{n} - (\hat{n} \cdot \hat{z})\hat{z}$ within the layers and does not possess intralayer inversion symmetry. Thus, the Sm-A_B^{*} phase has symmetry between the Sm-A* and Sm-C* phases. The chirality of the Sm-A_B^{*} phase means that the biaxial director \hat{e}_1 helically precesses along \hat{z} with pitch p_B . This precession may seem similar to the that of the Sm-C* phase in which \mathbf{c} precesses with pitch p_C . However, it will be shown to involve a fundamentally different helical distortion (twist) than that of Sm-C* phase (bend). Twist is a lower energy distortion than bend, which explains why the Sm-A_B^{*} pitch is shorter than the lower temperature Sm-C* phase. We show that p_B is up to a factor of K_b/K_t shorter than p_C , where K_b and K_t are the nematic twist and bend elastic moduli. Since K_b/K_t is typically of order 2 (and is often more), the Sm-A_B^{*} pitch will be considerably smaller than the Sm-C* pitch.

The Bragg reflections associated with the helical superstructure of the Sm-A_B^{*} and Sm-C* (or Sm-C_α^{*}) phases can be distinguished by comparing normal incidence (along \hat{z}) and oblique incidence scattering. Due to the intralayer inversion symmetry the actual periodicity of the orientational order and associated optical properties of the Sm-A_B^{*} phase will be $p_B/2$. This is unlike the Sm-C* phase, which lacks this inversion symmetry and is periodic only over the full pitch p_C . It is known [2] that the p_C periodicity of the Sm-C* phase is only revealed for scattering at oblique incidence. As shown in Fig. 2, for normal incidence only Bragg reflections at wave vectors $2nq_0$ (with $q_0 = 2\pi/p_{C/B}$ and n an integer) are observed. Thus, in going from normal to oblique incidence, extra Bragg reflections at odd multiples of q_0 will be observed in the Sm-C* phase but not in the Sm-A_B^{*} phase. Correspondingly, if measurements are *only* made for oblique incidence one may mistake the Sm-A_B^{*} phase for a Sm-C* phase with pitch

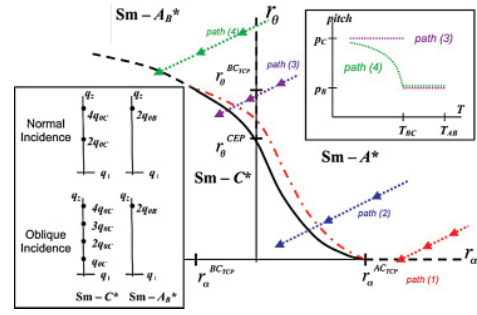


FIG. 2. (Color online) The phase diagram in r_α - r_θ space for the Sm-A*, Sm-A_B^{*}, Sm-C* phases. First- and second-order phase boundaries are shown as solid and dashed lines, respectively. Four decreasing temperature paths from the Sm-A* to Sm-C* phase are shown. In the region between the (black) solid and (orange) dot-dashed lines the system will exhibit a particularly dramatic electroclinic effect (see Fig. 3). (Top inset) The expected behavior of the helical pitch across the first- and second-order Sm-A_B^{*}-Sm-C* transitions. (Bottom inset) Schematic location of the normal or oblique incidence Bragg scattering wave-vector peaks associated with the helical superstructure of the Sm-A_B^{*} or Sm-C* phases, with $K_b/K_t \approx 2$. In the Sm-A_B^{*} phase there are only peaks at even multiples of q_{0B} for *both* normal and oblique incidence. In the Sm-C* phase the peaks are located at even multiples of q_{0C} for normal incidence but at integer multiples of q_{0C} for oblique incidence.

$p_B/2 = (K_t/2K_b)p_C$ that is significantly (by a factor of 4 or more) smaller than the actual Sm-C* phase that appears at lower temperature.

Another feature of the Sm-A_B^{*} phase is that its helical superstructure results in a decrease in the birefringence Δn from its Sm-A* value. A similar feature has been observed at the Sm-A*-Sm-C* and Sm-A*-Sm-C_α^{*} transitions and used to obtain $\theta(T)$ via measurements of $\Delta n(T)$ [11]. If a Sm-C_α^{*} phase was really a Sm-A_B^{*} phase then the indirect measurement of the Sm-C_α^{*} $\theta(T)$ may really be a measurement of the Sm-A_B^{*} biaxiality $\alpha(T)$.

The EE in the Sm-A_B^{*} phase is similar to that in a Sm-A* phase. Note that the EE in any Sm-A* phase will lead to *both* nonzero biaxiality and tilt. A signature of the second-order Sm-A*-Sm-A_B^{*} transition will be a discontinuity of $\frac{d\chi_0}{dT}$ but not a divergence of $\chi_0(T)$, where $\chi_0 = \frac{d\theta}{dE}|_{E=0}$ is the zero-field susceptibility. The rapid increase in χ_0 upon entry to the Sm-A_B^{*} phase, shown in Fig. 3, corresponds to an enhanced EE. In fact, $\frac{d\chi_0}{dT}$ will diverge as $T \rightarrow T_{AB-}$. This behavior at the Sm-A*-Sm-A_B^{*} transition is in contrast to that at the second-order Sm-A*-Sm-C* (or Sm-A*-Sm-C_α^{*}) transition where $\chi_0(T)$ diverges. Instead $\chi_0(T)$ diverges at the second-order Sm-A_B^{*}-Sm-C* transition. Thus, measuring $\chi_0(T)$ at the transition from the Sm-A* phase could distinguish the Sm-A_B^{*} and Sm-C_α^{*} phases.

If the Sm-A_B^{*}-Sm-C* transition is 1st order the divergence of $\chi_0(T)$ will be cut off. However, the EE will be dramatic above the transition temperature (T_{BC}) and akin to that of a Sm-A* phase near a first-order Sm-A*-Sm-C* transition [4,5]. As shown in Fig. 3, there is a superlinear growth of $\theta(E)$ and, below a critical temperature $T_E > T_{BC}$, discontinuities and hysteresis in $\theta(E)$ are expected (without switching the sign of E). Without (with) hysteresis one expects two/ (four)

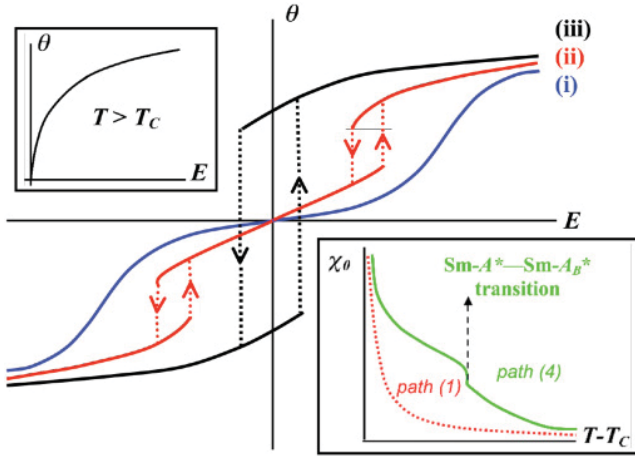


FIG. 3. (Color online) (Top inset) $\theta(E)$ in Sm-A* or Sm-A_B* phases above a continuous transition to the Sm-C* phase. The susceptibility χ_0 is the slope of the $\theta(E)$ curve at $E = 0$. (Bottom inset) $\chi_0(T)$ for phase sequences Sm-A*-Sm-C* (red dotted line) or Sm-A*-Sm-A_B*-Sm-C* (green solid line). Paths (1) and (4) refer to Fig. 2. The continuous transition to the Sm-C* phase is at T_C . For a first-order transition the divergence of $\chi_0(T)$ is cut off at $T > T_C$. (Main panel) $\theta(E)$ curves (i) and (ii) are in the Sm-A_B* phase above a first-order Sm-A_B*-Sm-C* transition at T_{AB} . (i) is above the critical temperature $T_E > T_{AB}$ and (ii) is at $T_{AB} < T < T_E$ (see Fig. 2 for the corresponding region in the phase diagram). Curve (iii) is in the Sm-C* phase, below a second- or first-order transition.

associated polarization current peaks instead of one/ (two) peaks for a surface stabilized Sm-C* phase. This unusually strong EE has also been observed [14,15] above the Sm-C_α*-Sm-C* transition and is generally attributed to a competition between ferro- and antiferroelectricity in the Sm-C_α* phase. If a Sm-C_α* phase was to be misidentified as a Sm-A_B* phase then such EE behavior could be due instead to the proximity of the first-order Sm-A_B*-Sm-C* transition.

We now briefly describe our theory. First, we map out the phase diagram for the nonchiral Sm-A, Sm-A_B, and Sm-C phases. The corresponding phase diagram for a chiral system will differ quantitatively (e.g., the exact location of the phase boundaries) but not qualitatively; that is, the diagram's topology, the possible phase sequences, and the order (first or second) of the transitions will remain the same. Thus, for the sake of clarity, the effects of chirality will be considered only when analyzing the manifestly chiral features, that is, the helical superstructures and EE.

The Sm-A, Sm-A_B, and Sm-C phases can be distinguished by their second rank tensor orientational order parameter Q , which we express as a sum of uniaxial and biaxial parts: $Q_{ij} = \sqrt{\frac{3}{2}}S[\cos(\alpha)U_{ij} + \frac{\sin(\alpha)}{\sqrt{3}}B_{ij}]$, where $U_{ij} = n_i n_j - \frac{1}{3}\delta_{ij}$ is the uniaxial part and $B_{ij} = e_{1i}e_{1j} - e_{2i}e_{2j}$ is the biaxial part. Taking the smectic layer normal to point along \hat{z} , the eigenvectors are $\hat{e}_1 = -\sin\phi(z)\hat{x} + \cos\phi(z)\hat{y}$, $\hat{e}_2 = \cos\theta[\cos\phi(z)\hat{x} + \sin\phi(z)\hat{y}] - \sin\theta\hat{z}$, and $\hat{n} = \sin\theta[\cos\phi(z)\hat{x} + \sin\phi(z)\hat{y}] + \cos\theta\hat{z}$. They and the angles ϕ and θ are shown in Fig. 1. The parameter α corresponds to the degree of biaxiality. The overall orientational order is $S = \sqrt{\text{Tr}(Q^2)} > 0$. The Sm-A phase is untilted ($\theta = 0$) and uniaxial ($\alpha = 0$). The Sm-A_B phase is

untilted ($\theta = 0$) and biaxial ($\alpha \neq 0$) while the Sm-C phase is tilted ($\theta \neq 0$) and biaxial ($\alpha \neq 0$). In the Sm-A_B* or Sm-C* phases, a helical superstructure corresponds to $\phi(z) = 2\pi z/p$ with p the pitch.

To analyze the transitions between the three phases we use a mean field Landau free energy density which, to lowest order in α and θ , is

$$f = \frac{r_\theta}{2}\theta^2 + \frac{u}{4}\theta^4 + \frac{\theta^6}{6} + \frac{r_\alpha}{2}\alpha^2 + \frac{\alpha^4}{4} - \gamma\alpha\theta^2. \quad (1)$$

$r_\theta(T)$ and $r_\alpha(T)$ are monotonically increasing functions of T , for example, $r_\alpha(T) = a_\alpha(T - T_\alpha)$ and $r_\theta(T) = a_\theta(T - T_\theta)$, where $a_\alpha, a_\theta > 0$, and T_α, T_θ are the temperatures below which, for zero coupling ($\gamma = 0$), α and θ each become nonzero. The coupling term's structure, linear in α and quadratic in θ , is important. It reflects the fact that if the system has tilt order, then by symmetry it must also have biaxial order, but not vice versa. Both $u, \gamma > 0$ but the coupling term will effectively reduce the θ^4 coefficient, even making it negative. Thus, the θ^6 term is required to stabilize the system. The simple form of the θ^6 and α^4 coefficients is achievable by rescaling θ and α . We note that the above f can be obtained by directly expanding in powers of Q_{ij} and a smectic layering order parameter, an approach which was taken in [5]. However, for the sake of brevity we do not take this approach here.

The phase diagram in r_α - r_θ space, shown in Fig. 2, is obtained by minimizing f with respect to α and θ . There are two tricritical points (TCPs), at each of which first- and second-order phase boundaries (for the Sm-A-Sm-C and Sm-A_B-Sm-C transitions) meet, as well as a critical end point (CEP) where the continuous Sm-A-Sm-A_B, first-order Sm-A-Sm-C and Sm-A_B-Sm-C boundaries meet. Reducing T corresponds to moving from upper right to lower left. There are four qualitatively different paths. Paths (1) and (2) do not involve a Sm-A_B phase and exhibit second- and first-order Sm-A-Sm-C phase transitions, respectively. The Sm-A_B phase appears along paths (3) and (4), each with a continuous Sm-A-Sm-A_B transition. The Sm-A_B-Sm-C transition is first and second order for paths (3) and (4), respectively.

We analyze the Sm-A_B* and Sm-C* helical superstructures by adding to f the term $f_{\text{chiral}} = -h\epsilon_{ijk}Q_{jl}\partial_i Q_{kl}$, where ϵ_{ijk} is the Levi-Cevita symbol. h depends on the enantiomeric excess and is zero in a racemic system. This term, which favors a chiral distortion, must be stabilized by the elastic terms, $f_{\text{elastic}} = \frac{k_t}{4}\partial_i Q_{jk}\partial_i Q_{jk} + \frac{k_b-k_t}{2}\partial_i Q_{ij}\partial_k Q_{kj}$, where k_t and k_b are proportional to the twist and bend elastic moduli; that is, $K_{t/b} = \frac{3}{2}k_{t/b}S^2$. In the Sm-A_B* or the Sm-C* phases $f_{\text{chiral}} + f_{\text{elastic}}$ is minimized by $\phi(z) = 2\pi z/p$ [16] with pitch $p(T)$:

$$p(T) = 2\pi \frac{k_t}{h} \left(\frac{1 + \kappa x^2(T)}{1 + x^2(T)} \right), \quad (2)$$

with $\kappa = k_b/k_t$ and $x(T) = \theta(T)/\alpha(T)$. In the Sm-A_B* phase ($\theta = 0$), $p = p_B = 2\pi k_t/h$. Setting $\alpha = 0$, one gets the usual uniaxial Sm-C* pitch $p_C = 2\pi k_b/h$. The ratio $p_C/p_B = K_b/K_t$ is the ratio of the energies of each helical distortion. In the Sm-A_B* phase the distortion is a twist of the biaxial director \hat{e}_1 . In the uniaxial Sm-C* phase the higher energy distortion is a bend of the uniaxial director \hat{n} . We note that the pitch lengths are equal in a one constant ($k_t = k_b$) approximation.

Generally, the Sm- C^* pitch lies between p_B and p_C . $p(T)$ for the sequence Sm- A^* –Sm- A_B^* –Sm- C^* , is summarized in Fig. 2. Upon entry to the Sm- A_B^* phase $p(T) = p_B$ and remains constant. Entering the Sm- C^* phase along path (4) (via a continuous Sm- A_B^* –Sm- C^* transition), $p(T)$ will increase continuously toward p_C as the $\theta^2(T)/\alpha^2(T)$ terms in Eq. (2) grow. Path (3) involves a first-order Sm- A_B^* –Sm- C^* transition where both α and θ jump. The most dramatic behavior occurs in the limiting case $u, \gamma \ll 1$, where $\theta^2 \gg \alpha^2$ upon entry to the Sm- C^* phase. Here $p(T)$ jumps, by a factor $\approx K_b/K_t$, up to $p \approx p_C$.

The reduction in birefringence Δn can be obtained by position averaging Q_{ij} over the helical pitch. Using $\Delta n \propto \text{Tr}(Q^2)$ we find that the fractional reduction in Δn , is

$$\Delta_{\Delta n}(T) = \frac{\alpha(T)^2}{2} + \frac{3\theta(T)^2}{2}. \quad (3)$$

Thus, as well as a decrease in Δn going from the Sm- A^* to the Sm- A_B^* phase, one will observe a decrease going from Sm- A_B^* to the Sm- C^* phase when $\theta(T)$ becomes nonzero. For a first-order transition one will observe a jump in $\Delta_{\Delta n}(T)$. The material 4-(1-methylheptyloxycarbonyl)phenyl 4'-octyloxybiphenyl-4-carboxylate (MHPOBC) shows the latter behavior [11]. Whereas Ref. [11] attributes this to some sort of structural change at the Sm- C_α^* –Sm- C^* transition, it could more simply attributed to the development of tilt order (in addition to biaxial order) at a first-order Sm- A_B^* –Sm- C^* transition.

Our analysis of the EE is preliminary in that we do not consider the role played in the EE by a possible helical superstructure. Keeping in mind that the layer normal points along \hat{z} , we add the following term to f : $f_{EE} = e' \epsilon_{zjk} E_j Q_{zk} \approx -e \mathbf{E}_\perp \cdot \hat{z}$, where $\mathbf{E}_\perp \perp \hat{z}$, $e = \sqrt{\frac{3}{2}} S e'$. For a racemic mixture $e' = 0$. The \approx means we do not consider effect of \mathbf{E} on α [17].

Two features of the EE are as follows. First, in the Sm- A^* and Sm- A_B^* phases, near the first-order transitions to the Sm- C^* phase (i.e., $T_{AC/BC} < T < T_E$), a discontinuous and hysteretic $\theta(E)$ (see Fig. 3) is observed. Figure 2 shows the locus in r_α – r_θ space corresponding to the critical temperature T_E . The second feature is the behavior of $\chi_0(T)$ in the phase sequence Sm- A^* –Sm- A_B^* –Sm- C^* . Outside the Sm- C^* phase, χ_0^{-1} (see Fig. 3), is

$$\chi_0^{-1} = \begin{cases} a_\theta(T - T_\theta) & T > T_{AB}, \\ a_\theta(T - T_\theta) - 2\gamma a_\alpha^{\frac{1}{2}}(T_{AB} - T)^{\frac{1}{2}} & T_{BC} < T < T_{AB}, \end{cases} \quad (4)$$

where $T_{BC} > T_\theta$ is the continuous Sm- A_B^* –Sm- C^* transition temperature, given by $\chi_0^{-1}(T_{BC}) = 0$. If the Sm- A_B^* –Sm- C^* transition is first order then the growth of $\chi_0^{-1}(T)$ is cut off at the transition ($T_{BC1st} > T_{BC}$). For a sequence Sm- A^* –Sm- C^* , $\chi_0^{-1} = a_\theta(T - T_\theta)$ in the Sm- A^* phase.

In summary, we have presented an analysis of the Sm- A_B^* phase, which has a helically precessing biaxial director. The helical pitch will be significantly shorter than that of the Sm- C^* phase. A decrease in the birefringence and a strengthening of the EE will be observed below the Sm- A^* –Sm- A_B^* transition. For systems with a first-order Sm- A_B^* –Sm- C^* phase transition, an unusually strong EE (with switching and hysteresis) will be observed in the Sm- A_B^* phase. The above features are shared by the Sm- A_B^* and Sm- C_α^* phases and we propose that it is possible that the Sm- A_B^* phase could be misidentified as the Sm- C_α^* phase. We have discussed ways to distinguish the two phases.

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